

Test; mult. choice + free resp. out of 108

- Rolle + MVT
- closed interval theorem
- how many rel max/min
- $f'$  when inc/dec
- concavity
- inflection point
- $\lim_{x \rightarrow a}$  question
- $f'$  graph w/ questions (like on board)
- justify max + min
- inflection points -  $f''$  changes signs or  $f'$  goes inc  $\rightarrow$  dec
  - MVT question
  - graph
- HA or VA question
- graph - inc/dec, concavity
- No proofs! (do have to justify answer) with words!

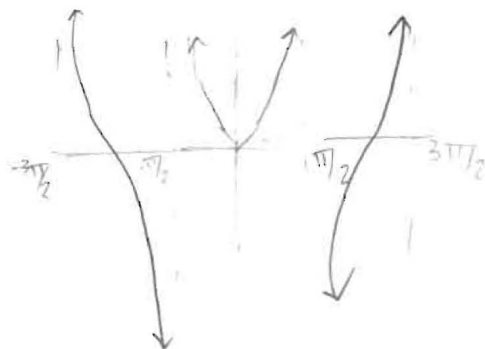
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#45.  $y = x \tan x \left( -\frac{3\pi}{2}, \frac{3\pi}{2} \right)$

$$y' = \frac{\tan x + x \sec^2 x}{\cos^2 x}$$

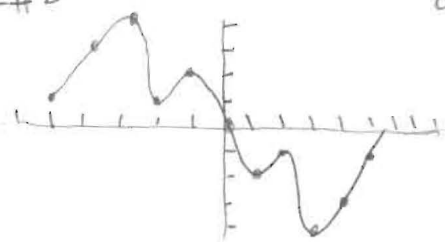
$$= \frac{\frac{1}{2} \sin 2x + x}{\cos^2 x}$$

rel. min (0, 0)  
VA  $k\pi$



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c.



odd, so can extrapolate points

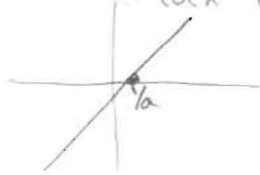
- Critical numbers

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$$f(x) = \frac{1}{2}(ax)^2 - (ax)$$

$$f'(x) = a^2x - a = a(ax - 1)$$

if  $a > 0$



dec  $(-\infty, \frac{1}{a})$  inc  $(\frac{1}{a}, \infty)$   
abs min  $(\frac{1}{a}, -\frac{1}{2})$

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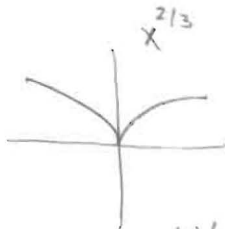
$$f(x) = y = 3(x-1)^{2/3} - (x-1)^2$$

$$(x-1)^{2/3} (3 - (x-1)^{4/3})$$

$$y' = 2(x-1)^{-1/3} - 2(x-1)$$

$$= 2(x-1)^{-1/3} (1 - (x-1)^{4/3})$$

$$= \frac{2(1 - (x-1)^{4/3})}{(x-1)^{1/3}}$$



• xint:  $(1, 0), (1 \pm \sqrt[4]{27}, 0)$

$$3 = (x-1)^{4/3}$$

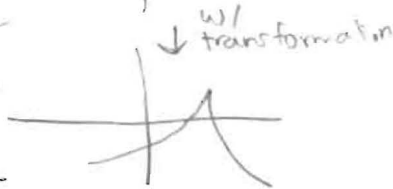
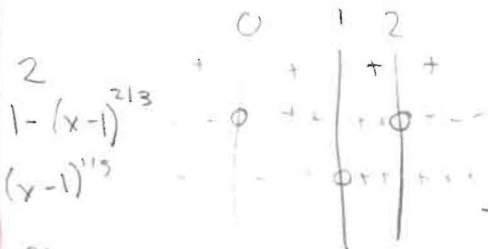
$$\pm \sqrt[4]{27} = x-1$$

$$x = 1 \pm \sqrt[4]{27}$$

• yint:  $(0, 2)$

• rel max  $(0, 2) (2, 2)$

• rel min  $(1, 0)$



f'

Ans

+++ 0 --- -/+ +0 ---

f

inc  $\cap$  dec  $\cup$  inc  $\cap$  dec

f(x)

